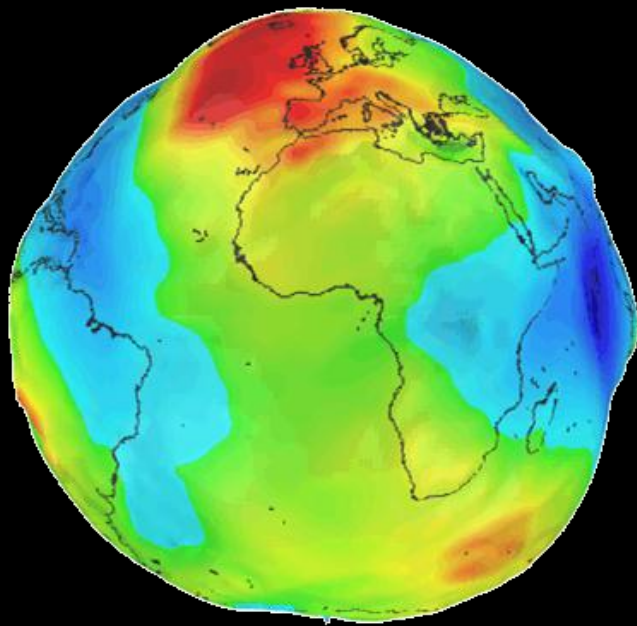


Earth's low degree gravitational variations from space geodetic data

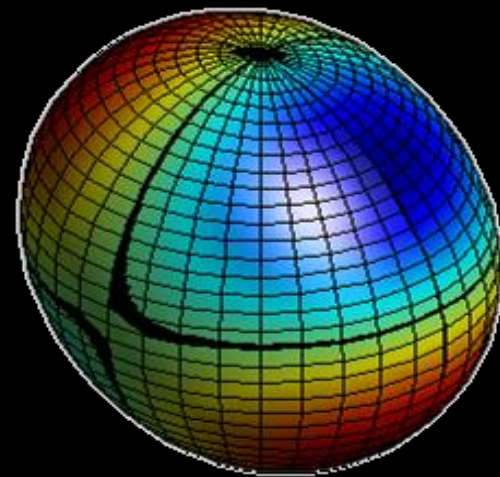
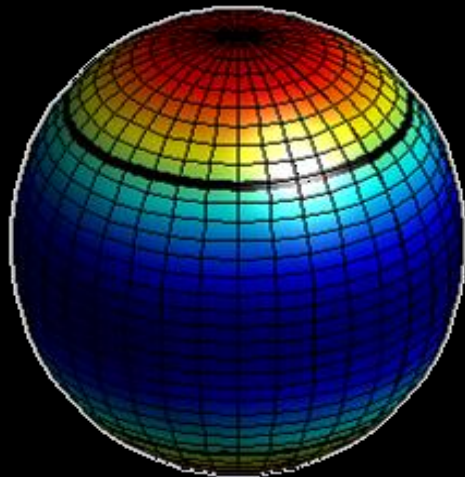


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- The C21, S21 and C20 Stokes coefficients are related to the Earth's principal figure axis and oblateness
- The redistribution of the mass within the Earth system induces changes in the Earth's gravity field.
- Mass load variations induce excitations in the EOPs that are proportional to those second-degree coefficients.
- SLR data are used to retrieve time series of direct estimates of low degree geopotential coefficients
- Time series of 2-deg Stokes coefficients can be derived from the EOP excitation functions (SLR and VLBI EOP in this study)



Geodetic Satellite Constellation

STELLA

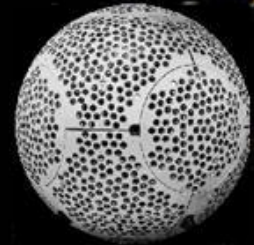
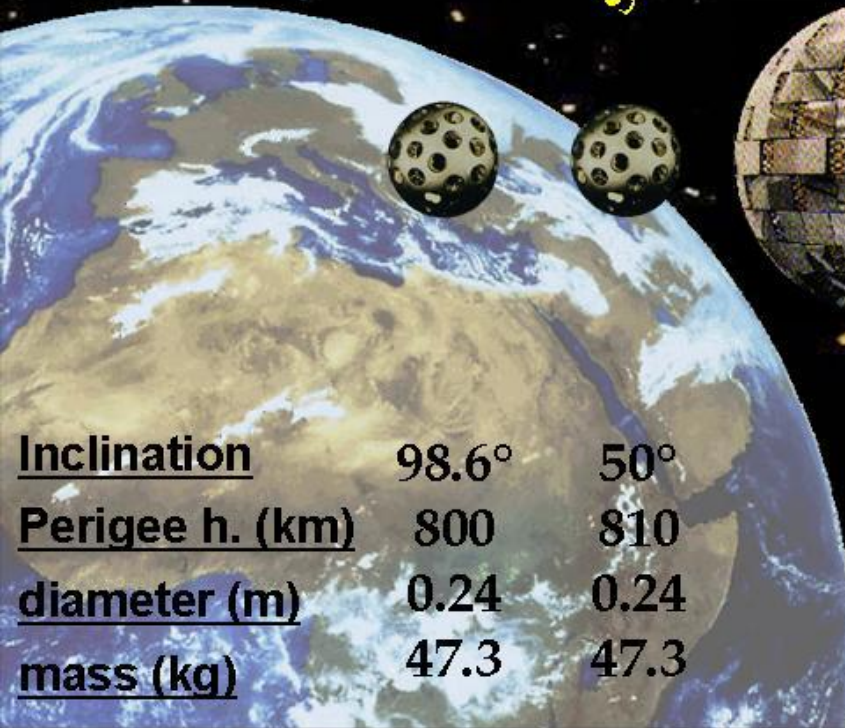
STARLETTE

AJISAI

LAGEOS-II

LAGEOS-I

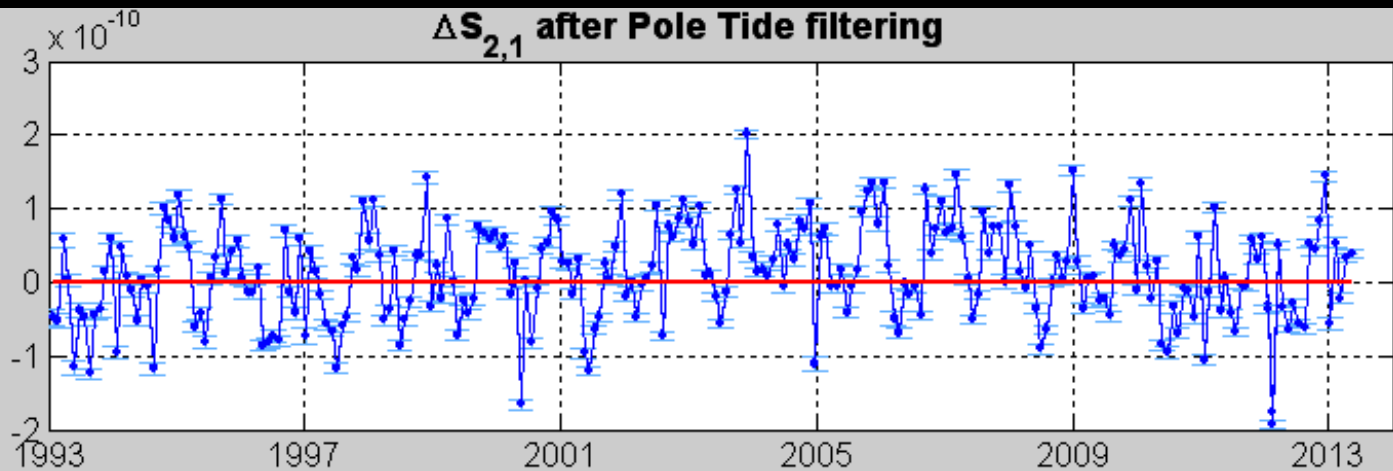
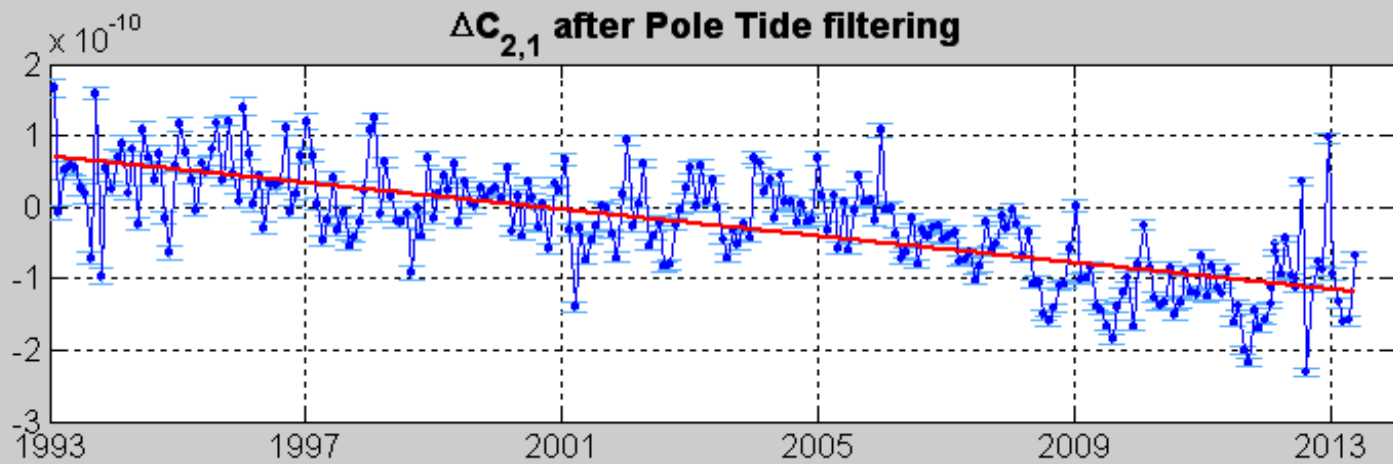
ETALON-I
ETALON-II



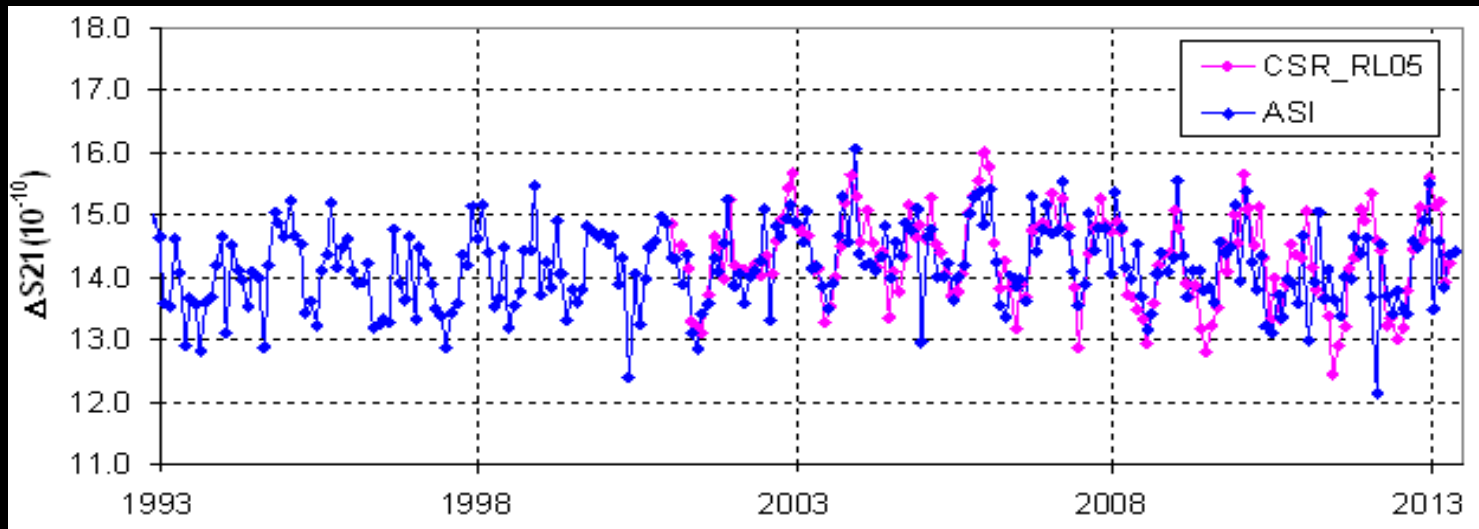
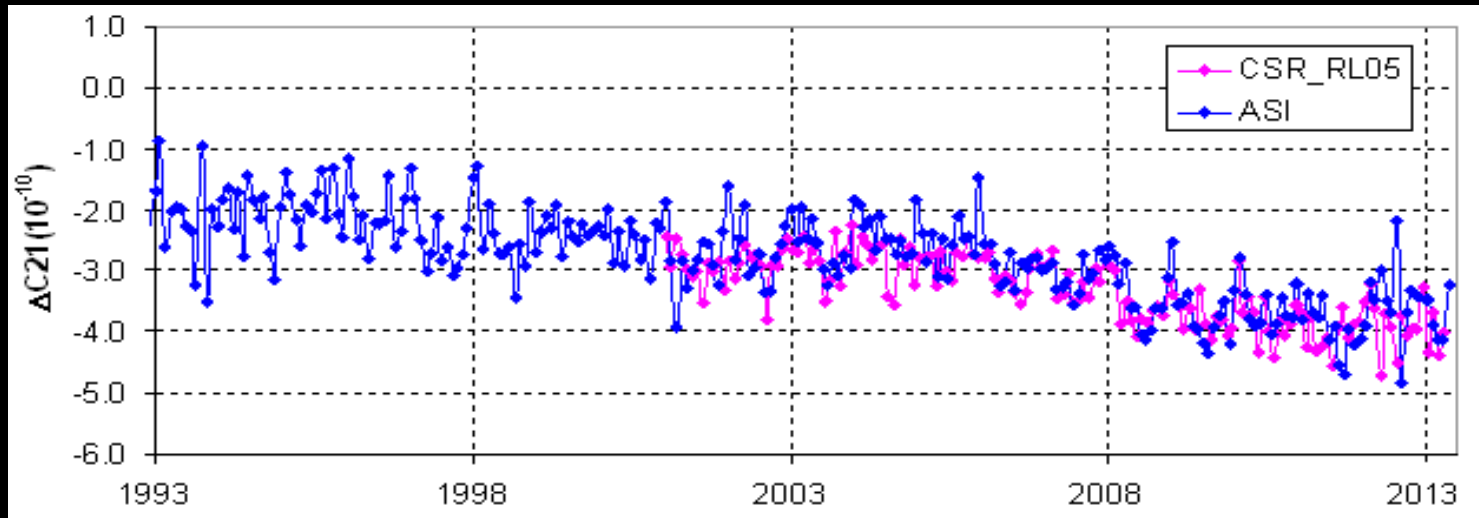
<u>Inclination</u>	98.6°	50°	50°	52.6°	109.8°	65.3°
<u>Perigee h. (km)</u>	800	810	1,485	5,620	5,860	19,105
<u>diameter (m)</u>	0.24	0.24	2.14	0.60	0.60	1.294
<u>mass (kg)</u>	47.3	47.3	685	405.4	407	1,415

All the SLR data available from 1983 to June 2013

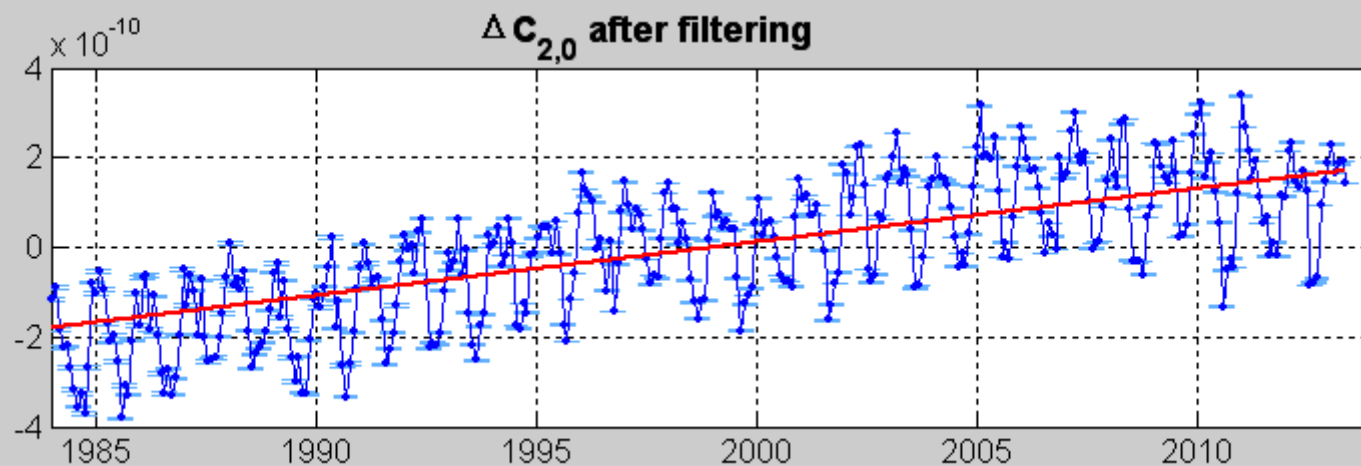
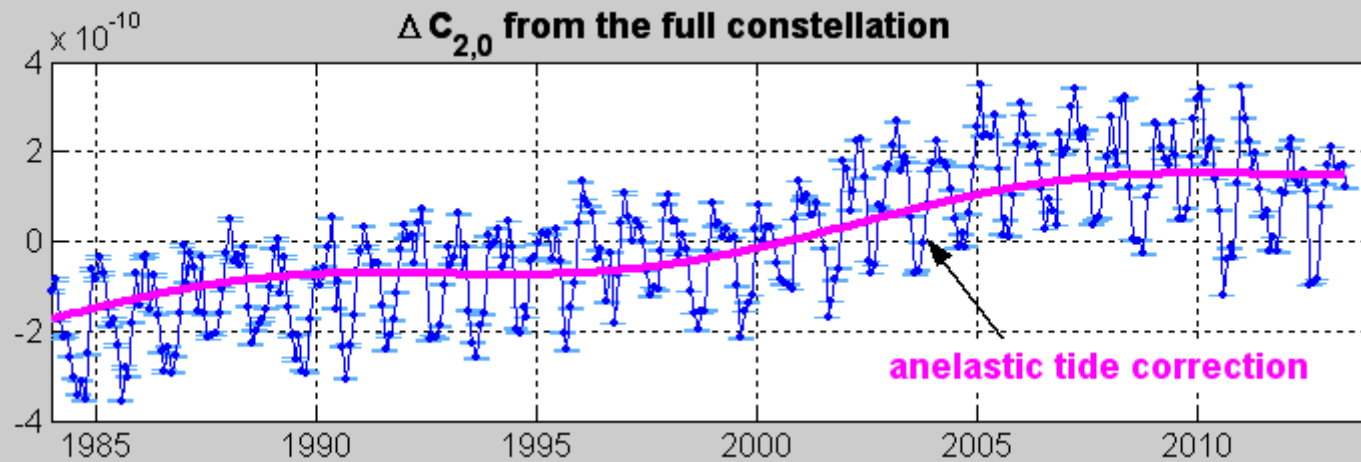
$\Delta C_{2,1}$ $\Delta S_{2,1}$ Full Time Series from SLR data



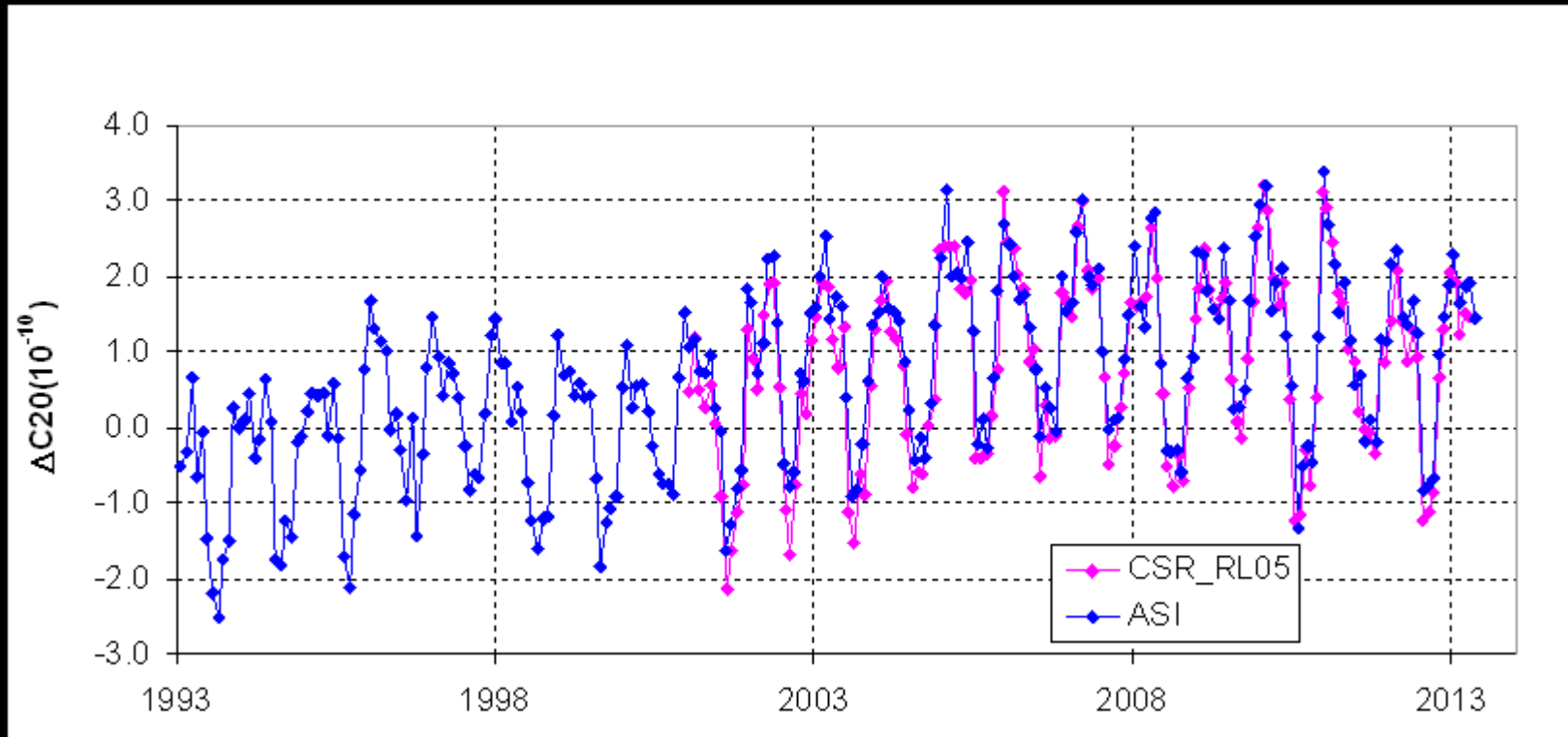
$\Delta C_{2,1}$ and $\Delta S_{2,1}$ external comparison



$\Delta C_{2,0}$ Time Series from SLR data



$\Delta C_{2,0}$ external comparison



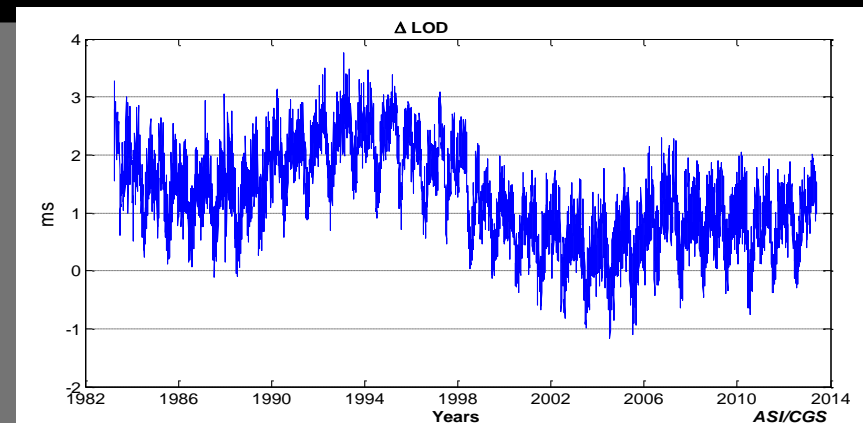
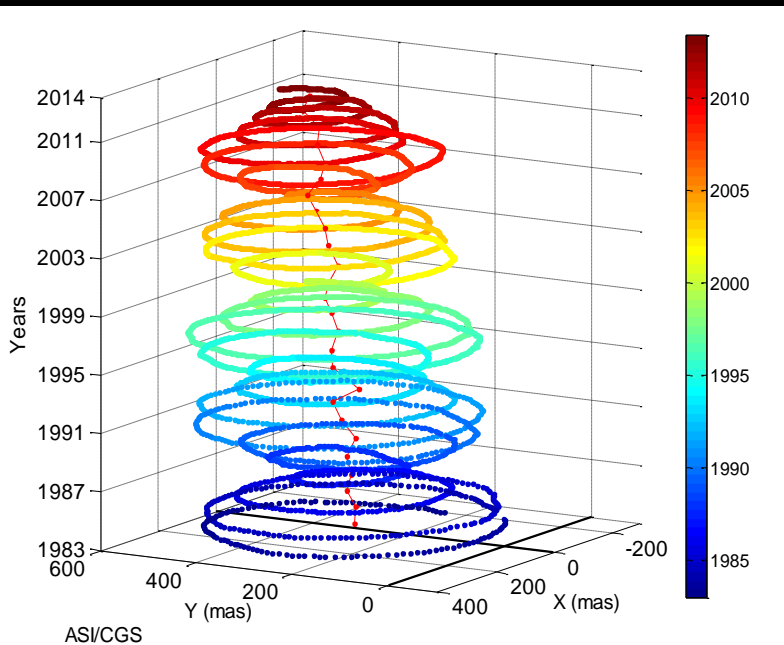
CSR solution:

Cheng, M. K., J. C. Ries, and B. D. Tapley (2011) Variations of the Earth's Figure Axis from Satellite Laser Ranging and GRACE, *J. Geophys. Res.*, 116, B01409, DOI:10.1029/2010JB000850.

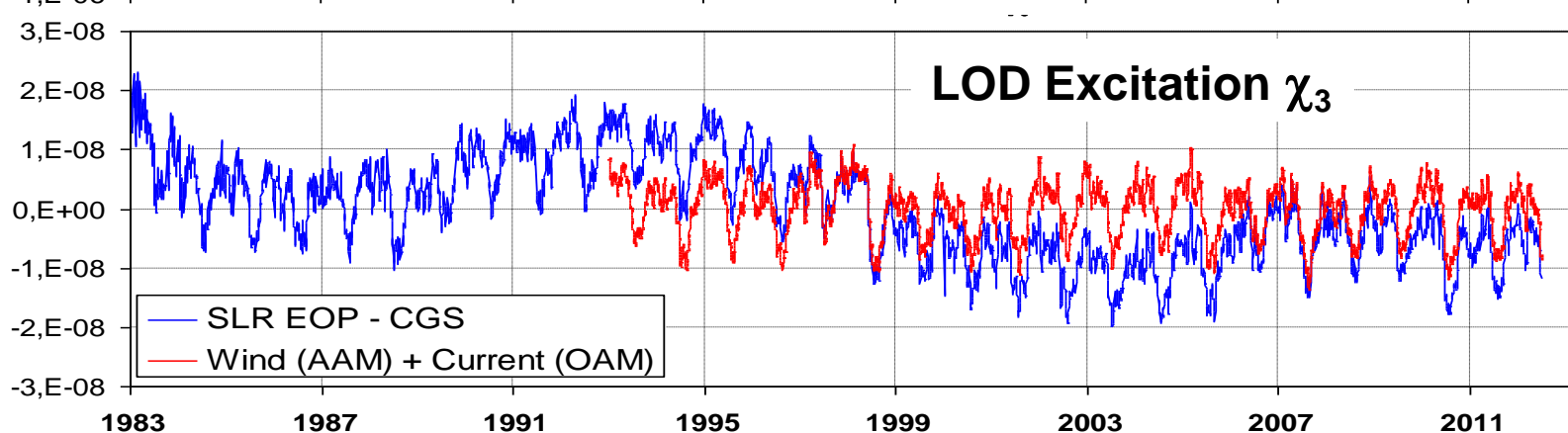
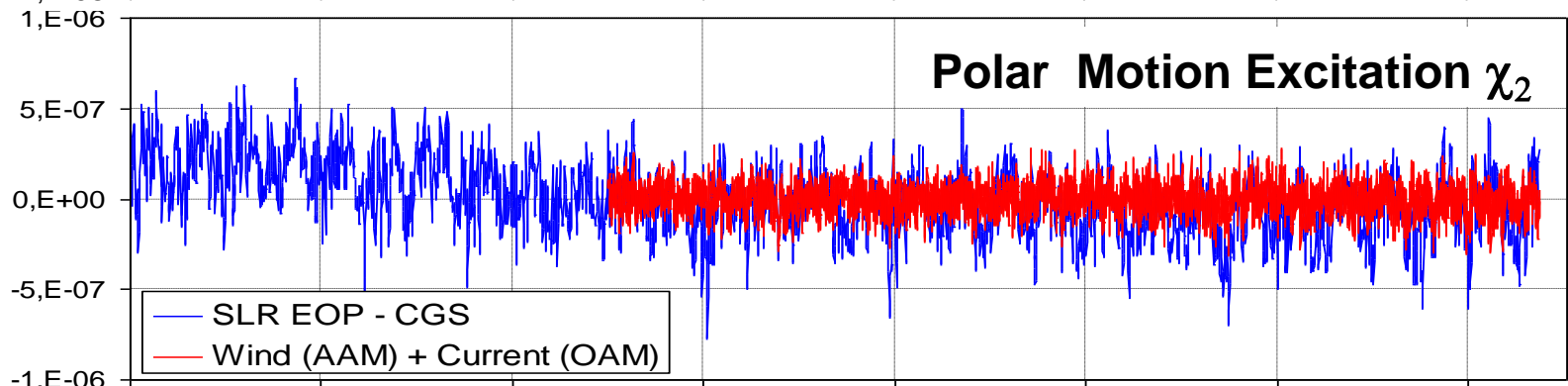
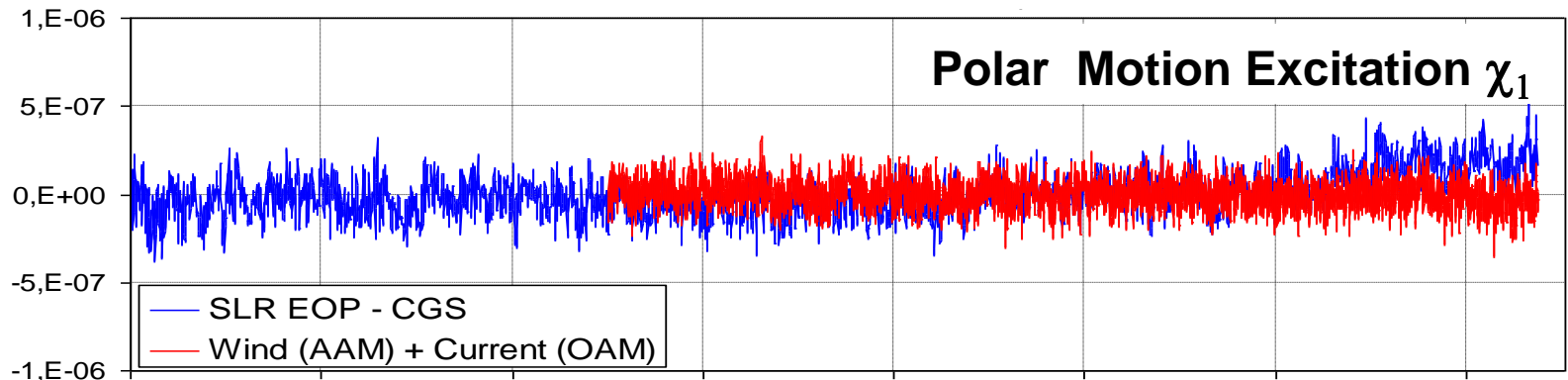
Polar motion and LOD

- Surface mass load variations induce excitations in the EOPs
- The excitation functions are proportional to the C_{21} , S_{21} and C_{20} coefficients
- Time series of excitation functions have been derived from the EOPs estimated at ASI/CGS from SLR (LAGEOS 1-2) and VLBI data and available at IERS as operational series

$$\Delta C_{21} + i\Delta S_{21} = -(1+k'_2)\sqrt{\frac{3}{5}} \frac{(C-A)}{1.098R^2M} (\chi_1^{mass} + i\chi_2^{mass}); \quad \Delta C_{20} = -(1+k'_2) \frac{3}{2\sqrt{5}} \frac{C_m}{0.753R^2M} \chi_3^{mass}$$



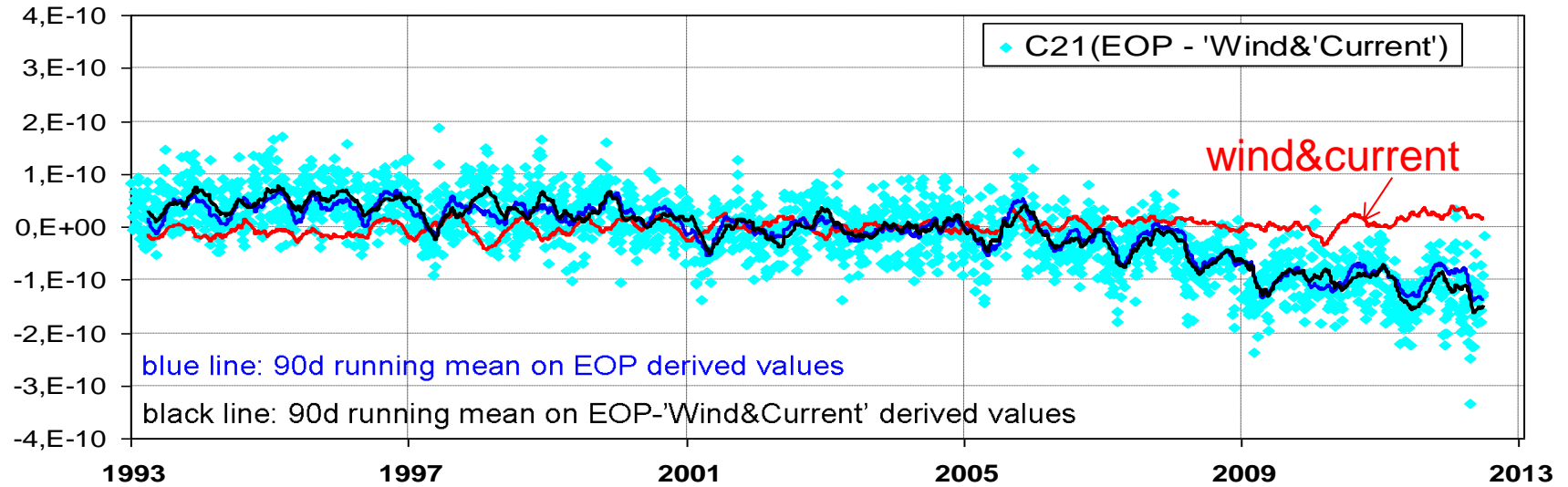
SLR Polar motion & LOD excitations



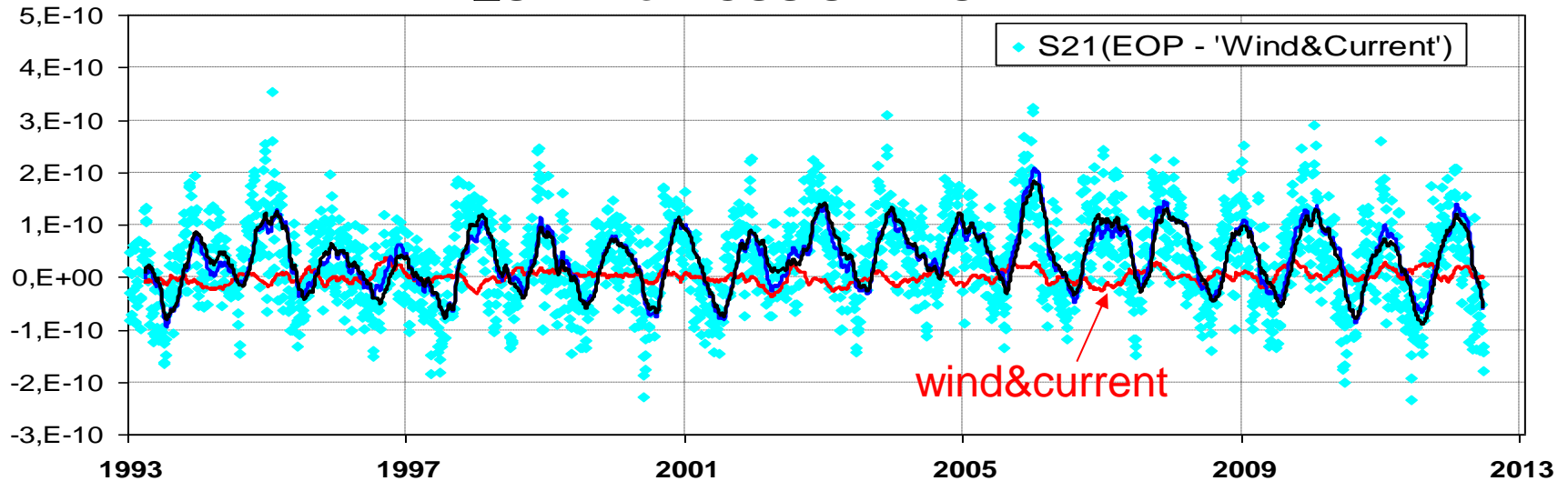
D. Salstein, aamf.ncep.reanalysis values, AER, IERS Special Bureau for the Atmosphere
R. Gross, ECCO_kf080.chi values, NASA/JPL, IERS Special Bureau for the Oceans

$\Delta C_{2,1}$ and $\Delta S_{2,1}$ from EOP

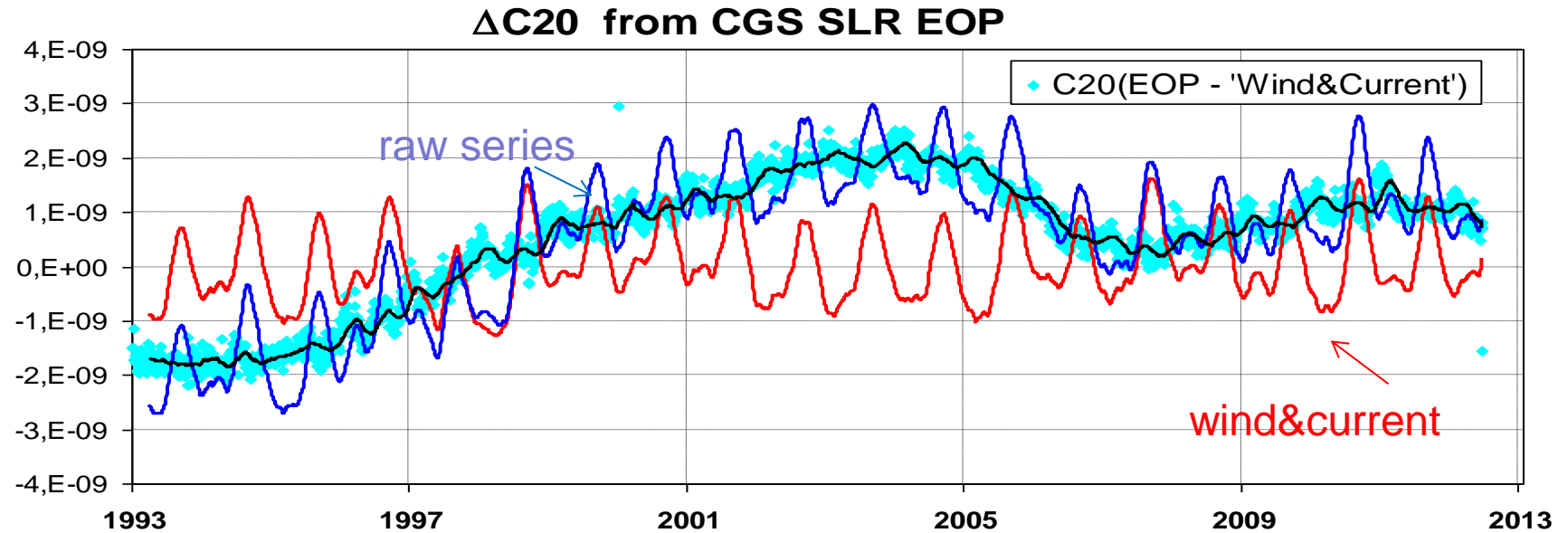
ΔC_{21} from CGS SLR EOP



ΔS_{21} from CGS SLR EOP



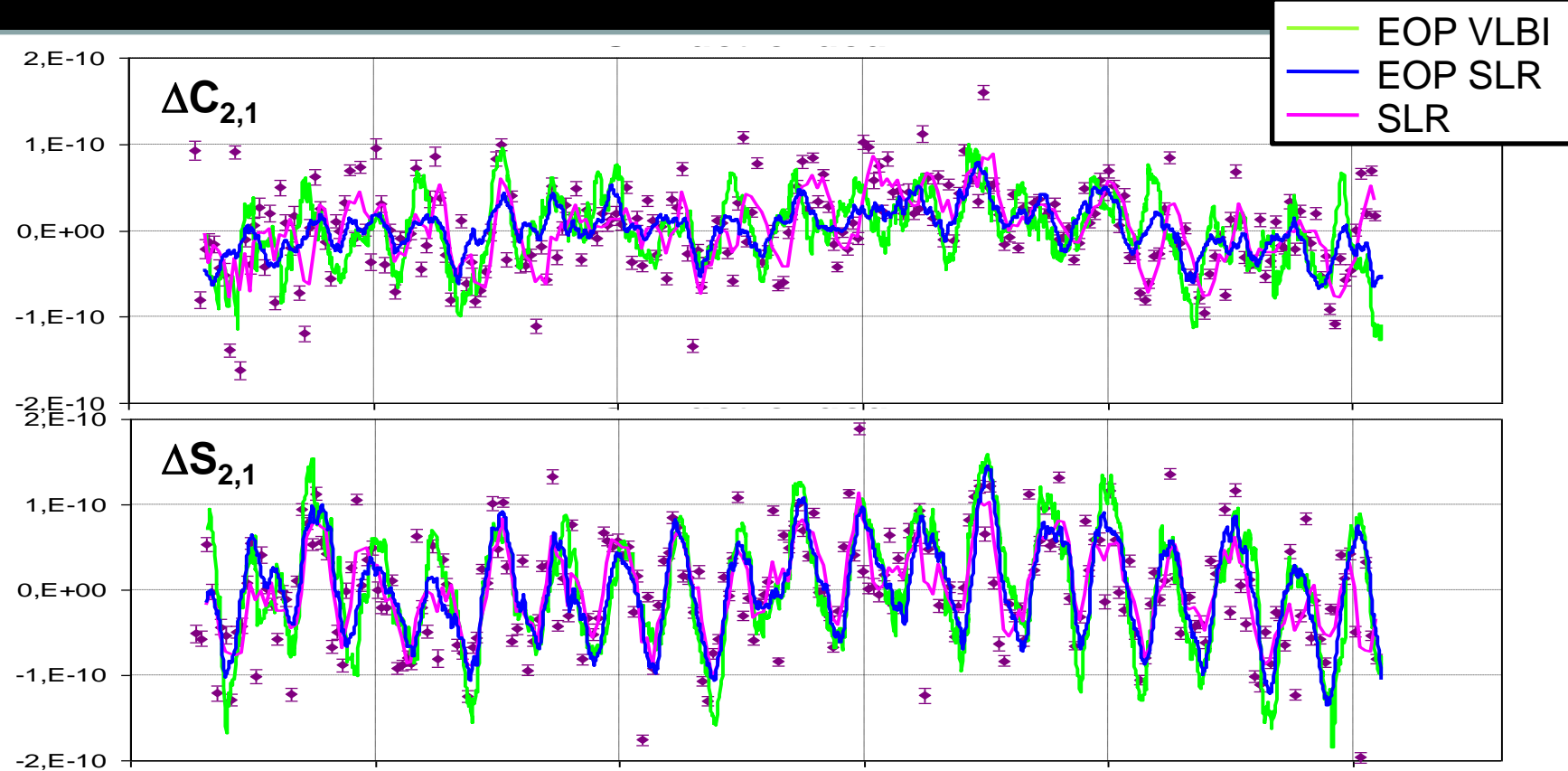
$\Delta C_{2,0}$ from EOP



blue line: 90d running mean on EOP derived values

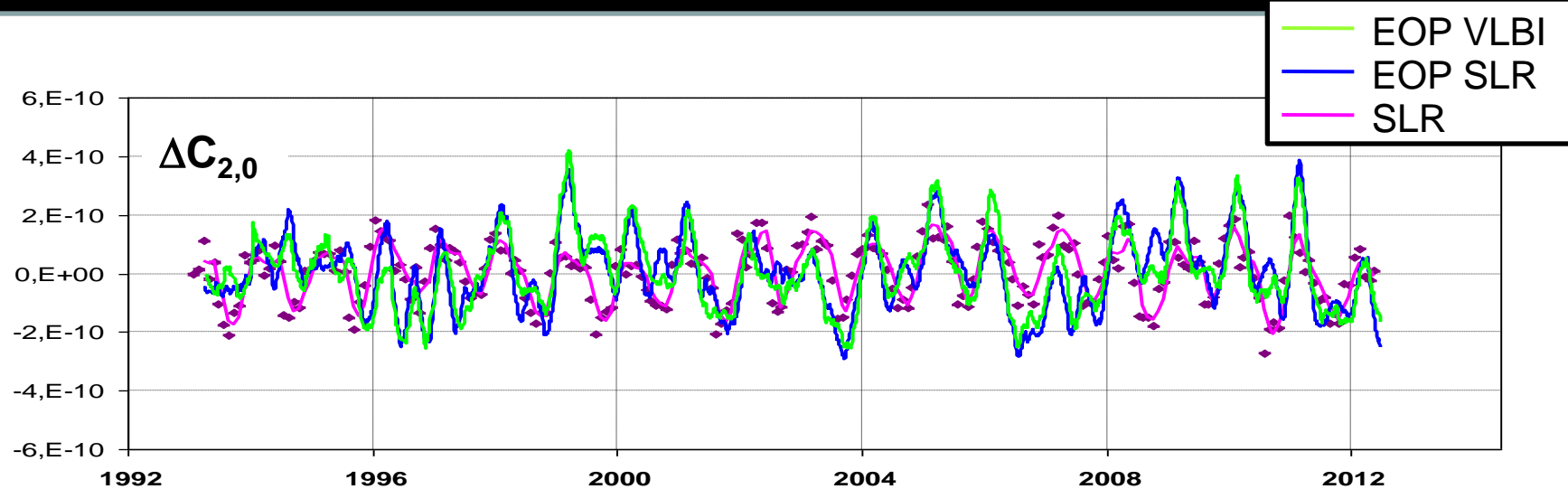
black line: 90d running mean on EOP-'Wind&Current' derived values

Comparison



- The residual behavior of C_{21} , S_{21} from SLR dynamics and from SLR & VLBI EOP excitation functions are similar.
- An annual frequency is clearly visible in all the terms, with more significant amplitude for S_{21} term.

Comparison

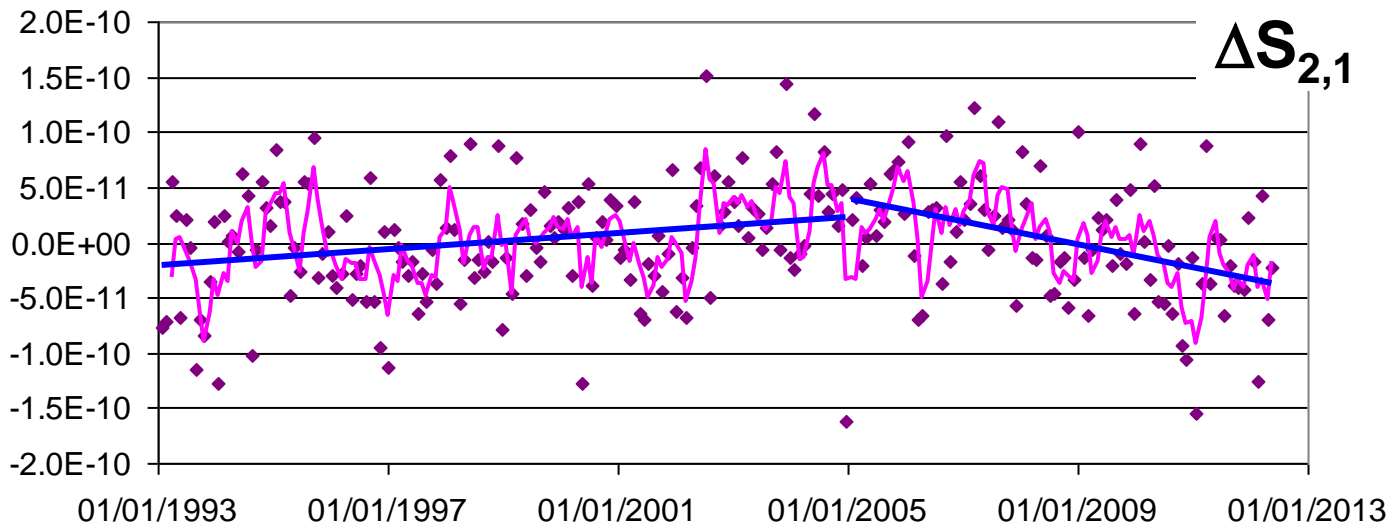
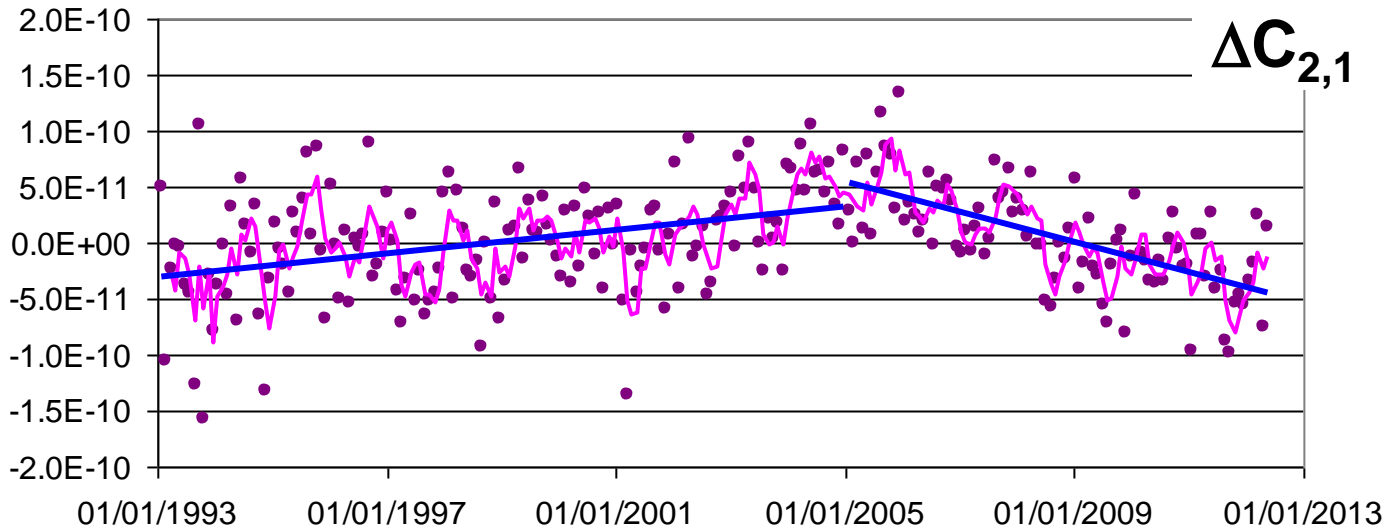


- The variations of C_{20} show similarities too, even if the interpretation of the direct comparison of the EOP derived series with the dynamics one is a bit more complicated: the LOD derived series, after the removal of the “motion” geophysical component, has been cleaned also from the low frequency terms ($<1/4 \text{ y}^{-1}$) and compared with the detrended C_{20} from SLR dynamics. Also in this case, a residual annual signature is visible in all the series.

“Numerical” summary

	Rate (10^{-12})	Annual amp (10^{-10})	Semi-annual amp (10^{-10})
$\Delta C_{2,1}$ SLR	-9.8 ± 0.6	0.25 ± 0.04	0.13 ± 0.04
$\Delta C_{2,1}$ EOP_SLR	-9.0 ± 0.2	0.22 ± 0.01	0.07 ± 0.01
$\Delta C_{2,1}$ EOP_VLBI	-9.1 ± 0.2	0.30 ± 0.02	0.06 ± 0.02
IERS conventions	-3.3		
$\Delta S_{2,1}$ SLR	0.7 ± 0.6	0.48 ± 0.05	0.11 ± 0.05
$\Delta S_{2,1}$ EOP_SLR	1.3 ± 0.2	0.71 ± 0.02	0.21 ± 0.02
$\Delta S_{2,1}$ EOP_VLBI	2.4 ± 0.2	0.77 ± 0.02	0.22 ± 0.02
IERS conventions	16.1		
$\Delta C_{2,0}$ SLR	10.6 ± 1.2	1.15 ± 0.05	0.38 ± 0.05
$\Delta C_{2,0}$ EOP_SLR	-	1.10 ± 0.05	1.01 ± 0.05
$\Delta C_{2,0}$ EOP_VLBI	-	1.16 ± 0.05	0.99 ± 0.05
IERS conventions	11.6		

Variations of the figure axis



Mean pole since 1900

