

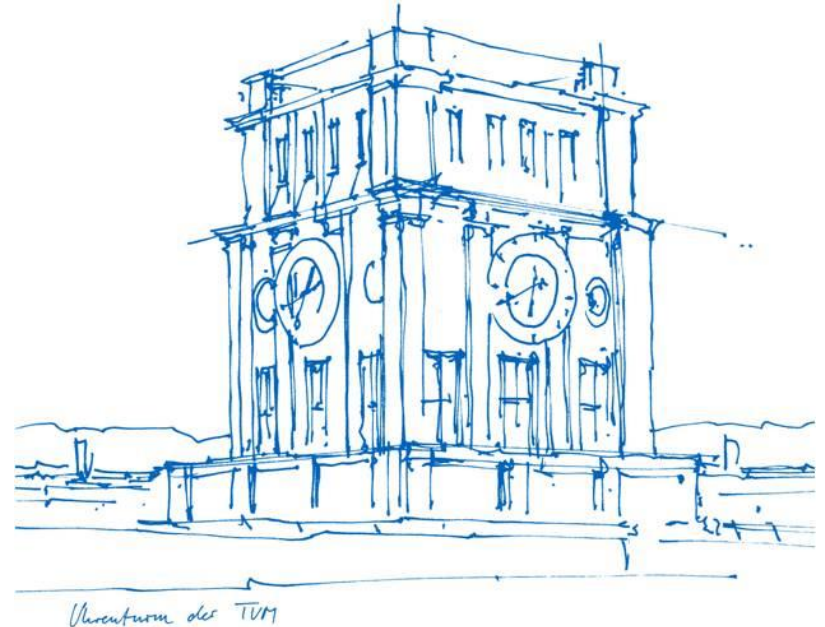
# Exploiting the synergy between optical two-way and microwave one-way ranging in a GNSS constellation

**Anja Schlicht, Stefan Marz**

TU München

22nd International Workshop on Laser Ranging

Jebes Spain



# Motivation: GGOS

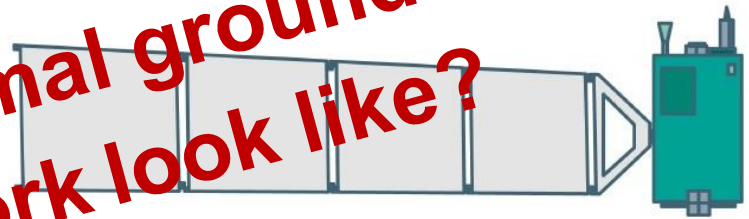
Co-location on ground

Co-location in space

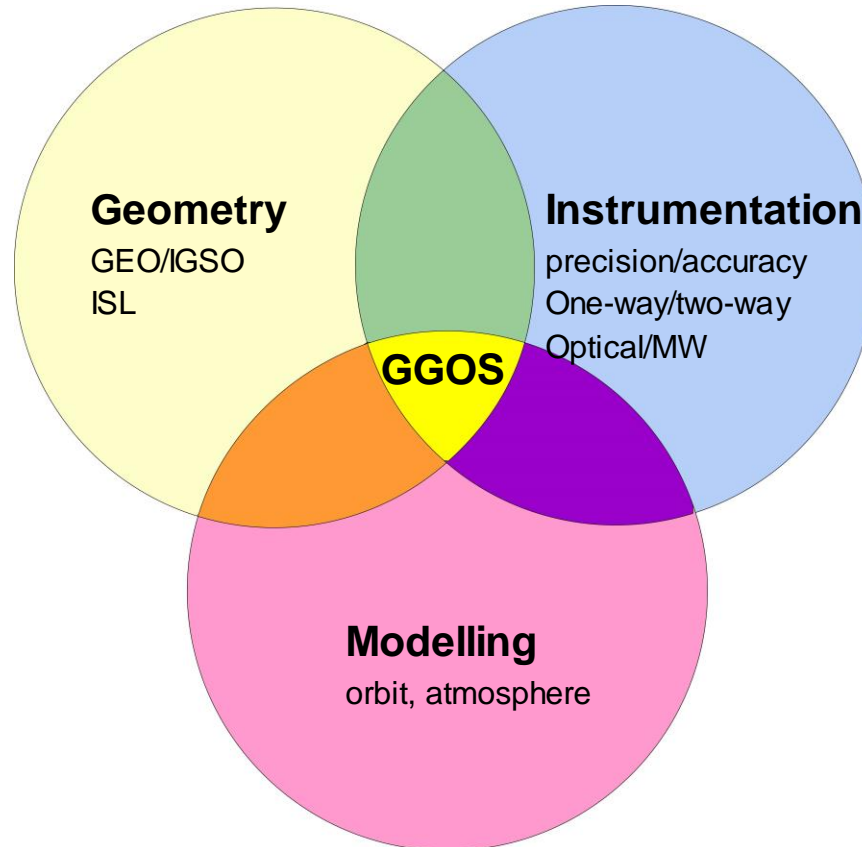


**How to combine?  
How would an optimal ground  
and satellite network look like?**

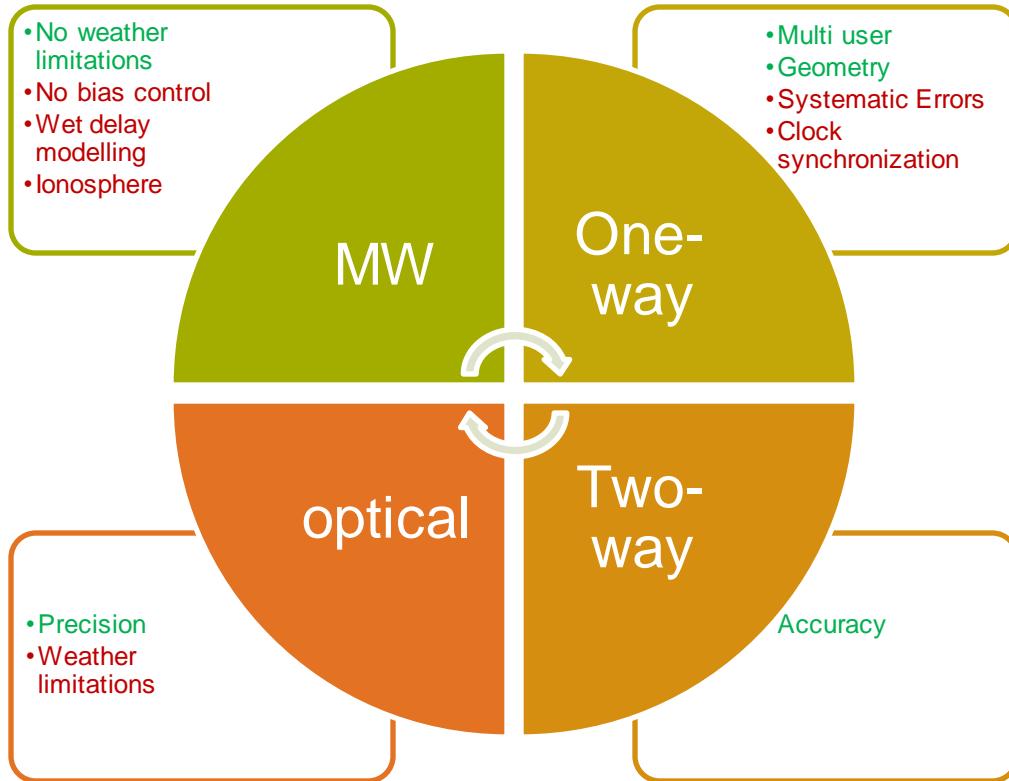
e.g. GENESIS



# Dependencies



# Ranging and Time Transfer Methods



## Inter-Satellite Links in GNSS:

- optical two-way 1 mm precision @ 30s,
- any-to-any scenario
- biases estimated

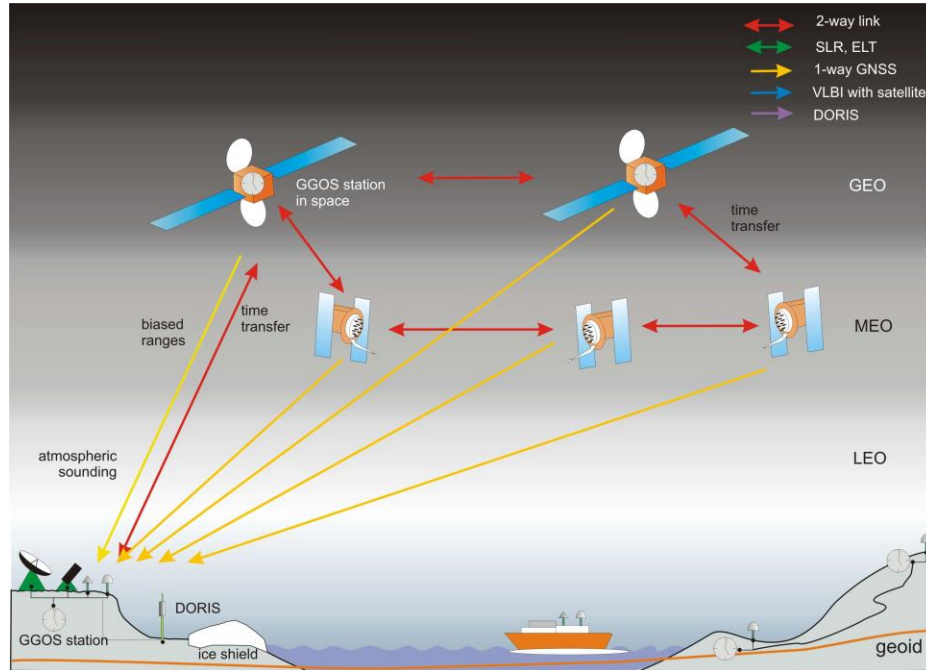
## Ground Links:

- co-located MW one-way and optical two-way 1 mm precision @ 30s
- time and range
- biases estimated
- **Common Troposphere Parameter estimation**

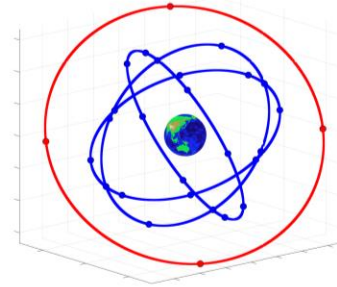
## Problem in combination:

- Weighting of measurements with great difference in number of observations, accuracy, and modelling parameters

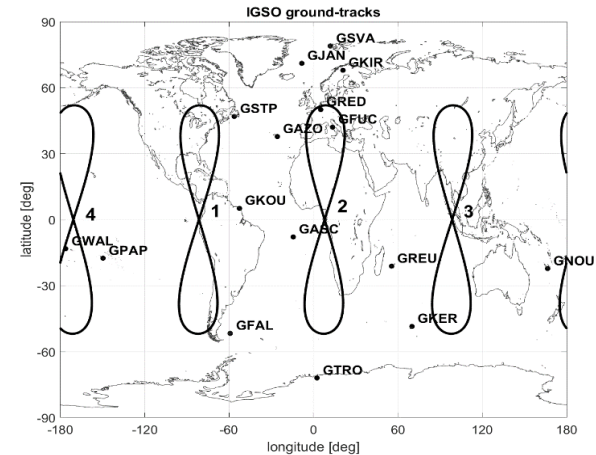
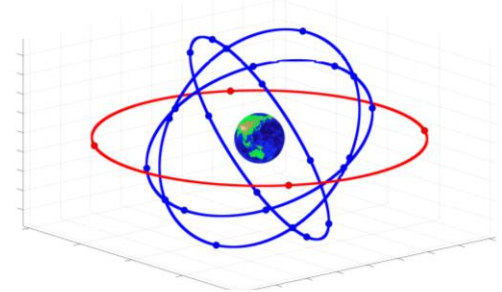
# Ranging methods, satellite constellations and ground station network



Galileo (blue) and IGSO (red) orbital planes in the ECI frame



Galileo (blue) and GEO (red) orbital planes in the ECI frame



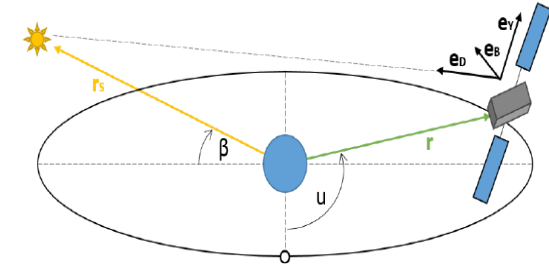
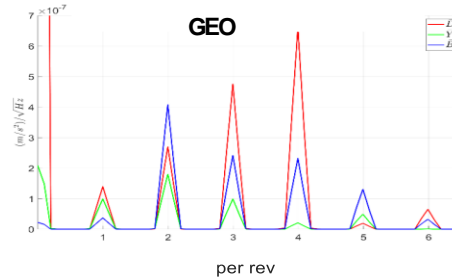
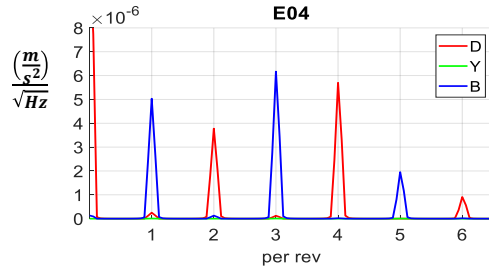
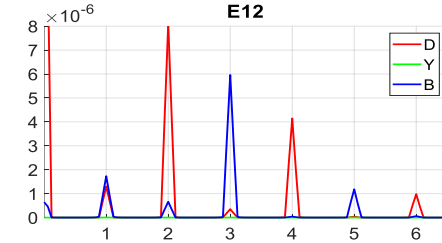
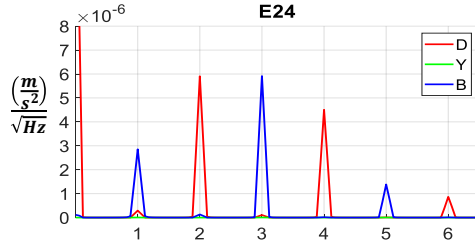
# Measurement Errors and Estimated Parameters

Simulated measurement errors	L-band	OTWL	OISL
White noise	<b>Yes</b> 15 cm for code, 1.5 mm for phase	<b>Yes</b> up to 0.5 mm	<b>Yes</b> up to 0.5 mm
Flicker noise (distance dependent)	<b>No</b>	<b>Yes</b> 1.2-1.4 mm (MEO), 1.7-1.9 mm (GSO)	<b>Yes</b> 0.1-1.5 mm (MEO and GSO)
Troposphere	<b>Yes</b>	<b>Yes</b>	-
PCV/Multipath	<b>Yes</b>	<b>No</b>	<b>No</b>
Constant bias	<b>Yes</b> up to 5 mm	<b>Yes</b> between $\pm 0.5$ mm	<b>Yes</b> between $\pm 0.5$ mm
Variable bias	<b>Yes</b> up to 5 mm	<b>Yes</b> between $\pm 0.5$ mm	<b>Yes</b> between $\pm 0.5$ mm

Estimated parameters per day	L-band	OTWL	OISL
Station specific tropospheric zenith delays	<b>Yes</b>	<b>No</b>	-
Ground station coordinates	<b>No</b>	<b>No</b>	-
Satellite initial state vectors and Solar Radiation Pressure (SRP) parameters	<b>Yes</b>	<b>Yes</b>	<b>Yes</b>
Epoch-wise satellite and ground station clock parameters	<b>Yes</b>	<b>Yes</b>	<b>Yes</b>
Phase ambiguities	<b>Yes</b>	-	-
Const. range and clock biases	<b>No</b>	<b>Yes</b>	<b>Yes</b>

# Solar Radiation Pressure Modelling

PSD of acceleration difference, 19043-19052



Acceleration error:  
wrong box-wing  
parameters

$$D = D_0 + D_{2c} \cos(2\Delta u) + D_{2s} \sin(2\Delta u) + D_{4c} \cos(4\Delta u) + D_{4s} \sin(4\Delta u)$$

$$Y = Y_0$$

$$B = B_0 + B_{1c} \cos(\Delta u) + B_{1s} \sin(\Delta u)$$

$$B = B_0 + B_{1c} \cos(\Delta u) + B_{1s} \sin(\Delta u) + B_{2c} \cos(3\Delta u) + B_{2s} \sin(3\Delta u)$$

$$B = B_0 + B_{1c} \cos(\Delta u) + B_{1s} \sin(\Delta u) + B_{2c} \cos(3\Delta u) + B_{2s} \sin(3\Delta u) + B_{3c} \cos(5\Delta u) + B_{3s} \sin(5\Delta u)$$

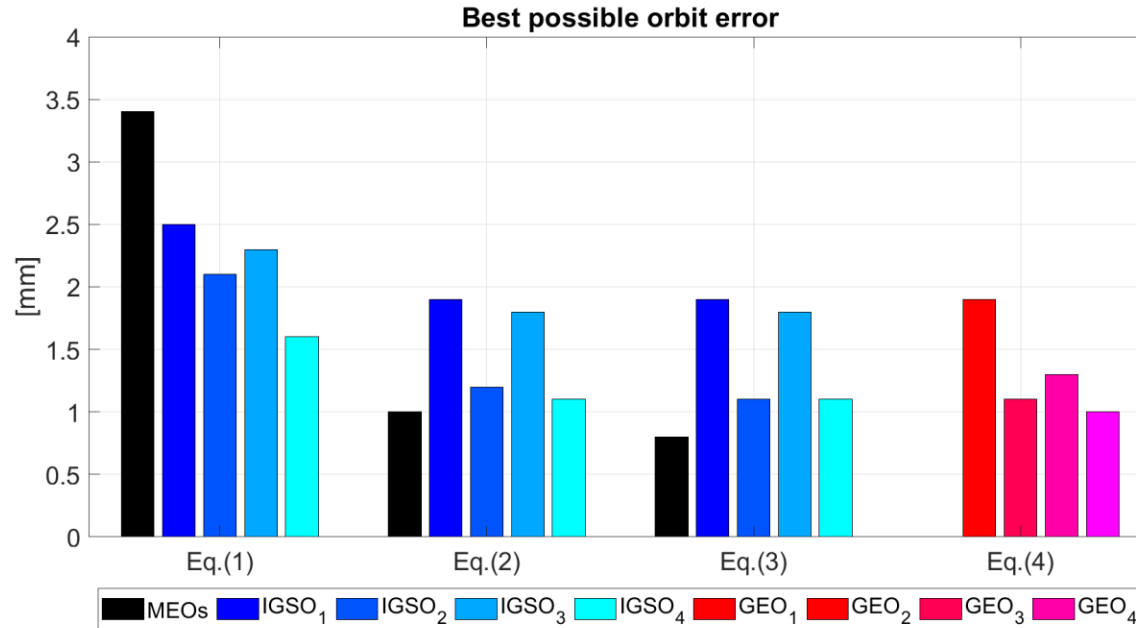
$$(1) \quad \bar{D} = \bar{D}_0 + \bar{D}_{1s} \sin(\Delta u) + \bar{D}_{2c} \cos(2\Delta u) + \bar{D}_{2s} \sin(3\Delta u) + \bar{D}_{4c} \cos(4\Delta u)$$

$$(2) \quad \bar{Y} = \bar{Y}_0 + \bar{Y}_{1s} \sin(\Delta u) + \bar{Y}_{2c} \cos(2\Delta u)$$

$$(3) \quad \bar{B} = \bar{B}_0 + \bar{B}_{1c} \cos(\Delta u) + \bar{B}_{2s} \sin(2\Delta u) + \bar{B}_{2c} \cos(3\Delta u) + \bar{B}_{4s} \sin(4\Delta u)$$

(4)

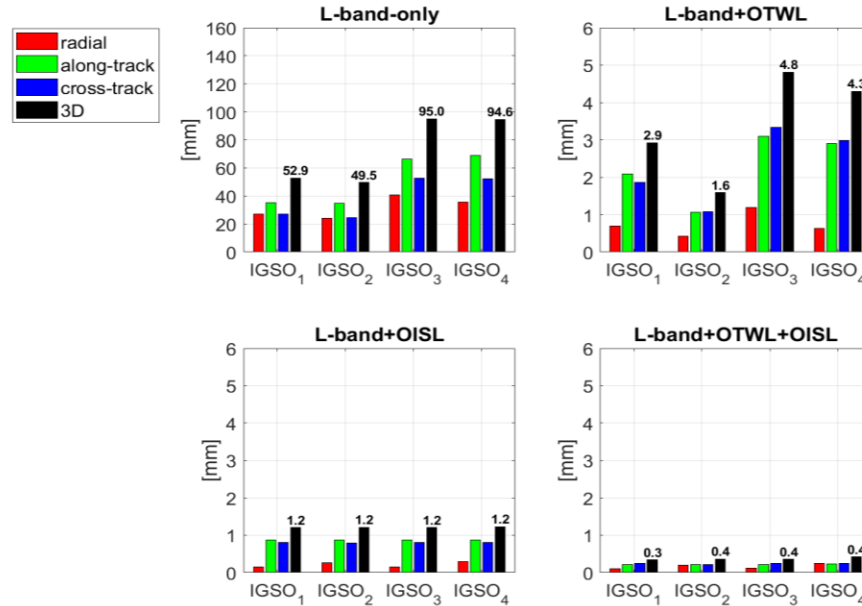
# Orbit Modelling Errors – Best possible Orbit





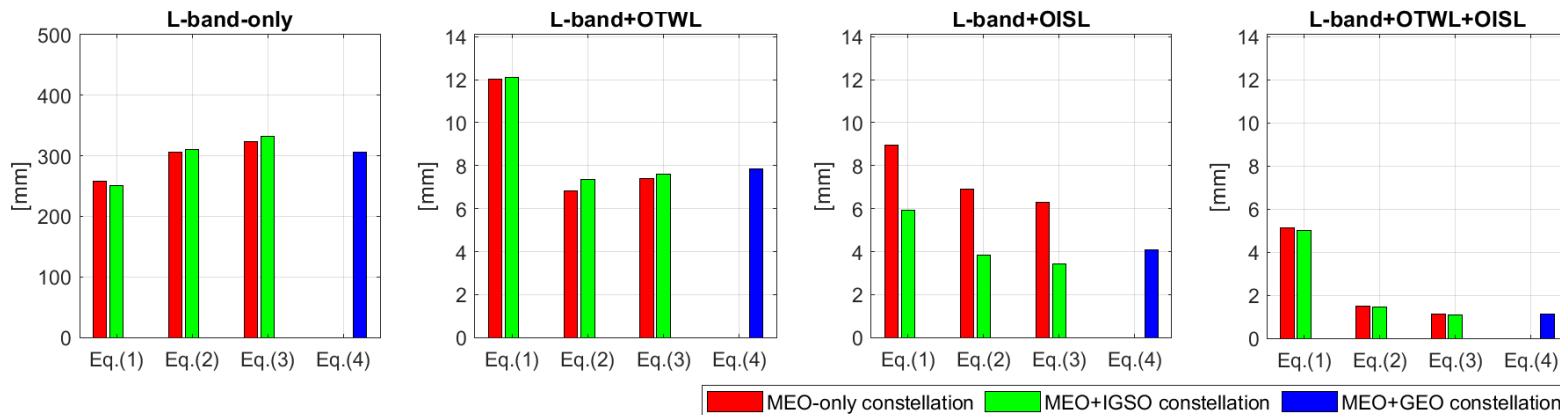
# Formal Errors – Influence of geometry and white noise

Formal orbit uncertainty of IGSO satellites, SRP modeling according to Eqn. (3)

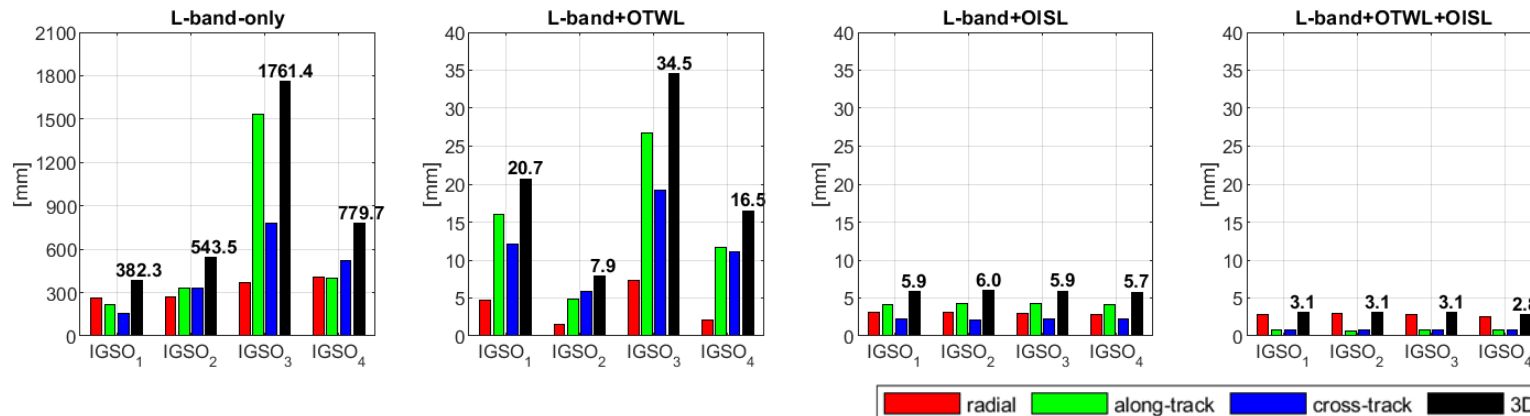


# Orbit Errors (no weather limitations in optical)

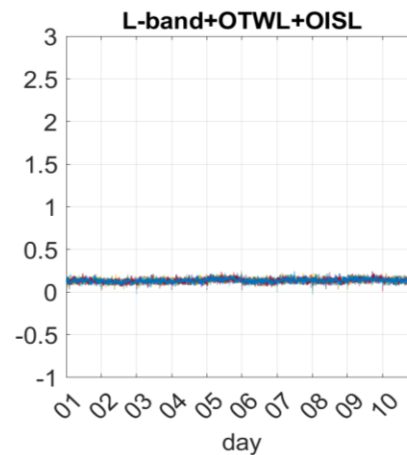
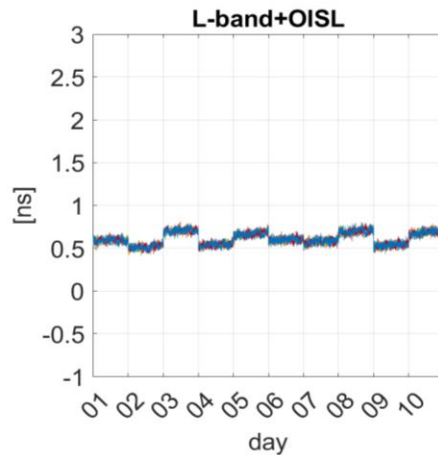
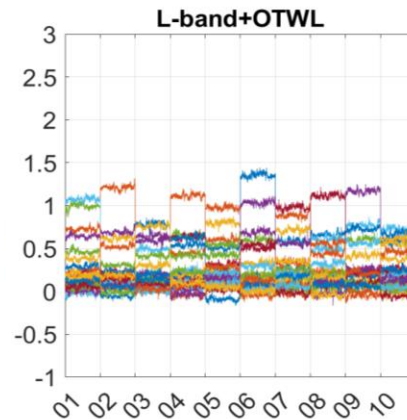
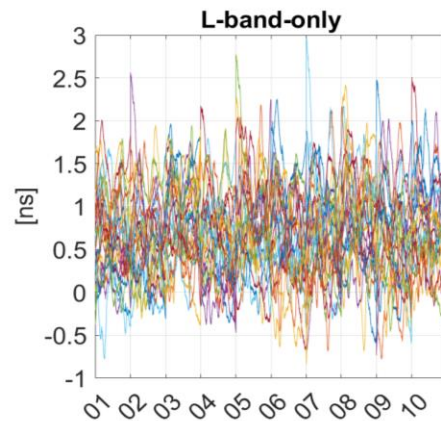
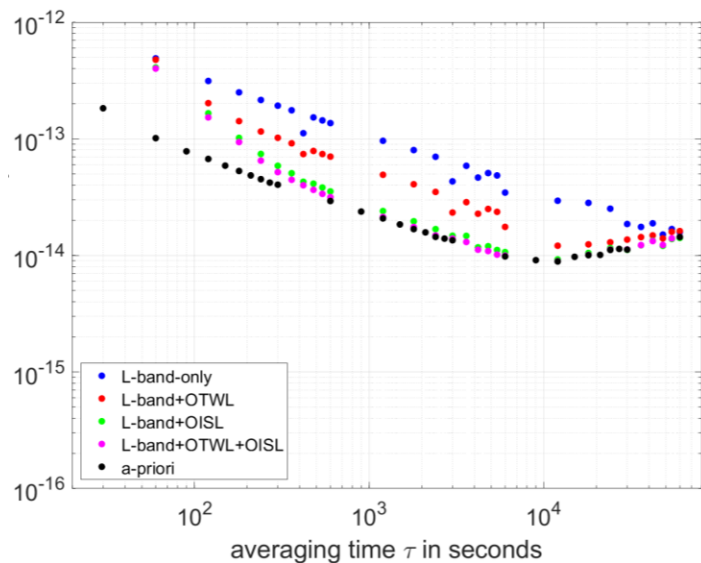
MEO



IGSO

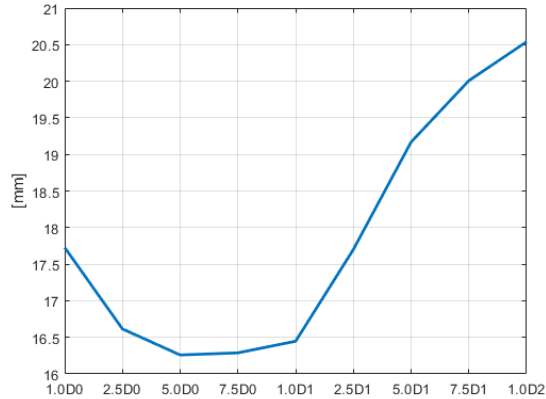


# Clock Errors

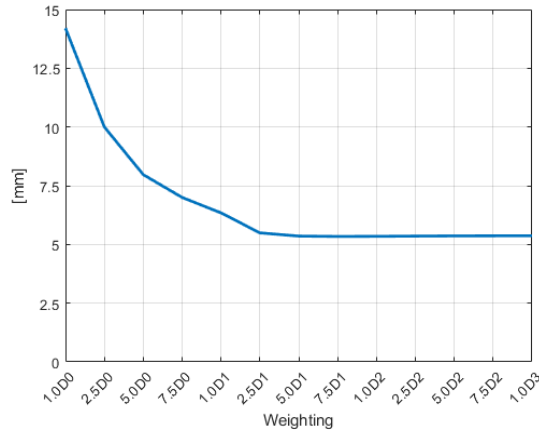


# Weighting

OISLECOM2  
Without GSO



OTWLECOM2+B3  
Without GSO



SRP modeling according to	with IGSO satellites			with GEO satellites		
	L-band + OTWL [mm]	L-band + OISL [mm]	L-band + OTWL + OISL [mm]	L-band + OTWL [mm]	L-band + OISL [mm]	L-band + OTWL + OISL [mm]
Eqn. (1)	25	2.5	2.5			
Eqn. (2)	25	25	25			
Eqn. (3)	25	25	25			
Eqn. (4)	-	-	-	100	100	10

# Future in navigation und time synchronization

